Multicore Computing

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OpenMP

- Open Multi-Processing
- An API that supports multi-platform shared-memory multiprocessing programming in C, C++, and Fortran

OpenMP: Quick Start

```
for (int i = 0; i < N;++i){
        b[i] = a[i] + 1;
}
```

OpenMP: Quick Start

```
#pragma omp parallel for schedule(static) num_threads(8)
for (int i = 0; i < N;++i){
        b[i] = a[i] + 1;
}
```

- g++ test.cc –fopenmp -o test -O2

- brew install libomp
- clang++ test.cc -o test -O2 -Xpreprocessor -fopenmp -I/usr/local/include -L/usr/local/lib -lomp

OpenMP: Quick Start

```
int sum = 0;


for (int i = 0; i < N; ++i){
        sum += a[i];
}
```

OpenMP: Quick Start

```
int sum = 0;
#pragma omp parallel for schedule(static) default(shared)
reduction(+:sum) num_threads(8)
for (int i = 0; i < N; ++i){
        sum += a[i];
}
```

OpenMP: Slow Start

- #include<omp.h>
- void omp_set_num_threads(int num_threads)
- int omp_get_num_threads()
- int omp_get_thread_num()

- #pragma omp atomic (update/read/write/capture)
- #pragma omp critical

Gauss-Seidel Smoother

- Solving PDE

- Parallel
- Synchronization
- Lock
- Communication

Matrix Multiplication (in Theory)

$$\begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} = \begin{bmatrix} A_{11}B_{11} + A_{12}B_{21} & A_{11}B_{12} + A_{12}B_{22} \\ A_{21}B_{11} + A_{22}B_{21} & A_{21}B_{12} + A_{22}B_{22} \end{bmatrix}$$

Matrix Multiplication (in Theory)

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Arithmetic intensity: the ratio of the work to the memory traffic

Strassen Algorithm

$$
\begin{aligned}
M_1 &= (A_{11} + A_{22})(B_{11} + B_{22});\\
M_2 &= (A_{21} + A_{22})B_{11};\\
M_3 &= A_{11}(B_{12} - B_{22});\\
M_4 &= A_{22}(B_{21} - B_{11});\\
M_5 &= (A_{11} + A_{12})B_{22};\\
M_6 &= (A_{21} - A_{11})(B_{11} + B_{12});\\
M_7 &= (A_{12} - A_{22})(B_{21} + B_{22}),
\end{aligned}
$$

$$
\begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} = \begin{bmatrix} M_1 + M_4 - M_5 + M_7 & M_3 + M_5 \\ M_2 + M_4 & M_1 - M_2 + M_3 + M_6 \end{bmatrix}
$$

HW 1: Logistic Regression

- Given matrix X and label Y, perform gradient descent of logistic regression
- 10 independent test cases. Each case weights 1 pt.

- The compilation is considered failed if it does not finish in 1 minute.
- A test case is considered incorrect if it does not finish in 2 minutes.
- The training accuracy must reach 60%.

- The summation of the execution time across 10 cases will be uses to rank correct solutions.

- Due: 02/02/2026 5:00 pm ET

Grading

- Homework 40%
- Reading 10%
- Project 50%

- 90%<=A<=100%
- 80%<=B<90%
- 70%<=C<80%
- 60%<=D<70%
- 0%<=F<60%

- 5 pieces of homework.
- No late submissions.
- No 3rd party code
- Automatically tested: Please strictly follow the output format. An incorrect format is considered as a wrong answer.
- The best 4 scores among the 5 are counted in your final grade.
- The fastest correct solution in each homework gets 10% bonus score in the final grade.
- Other correct solutions that are no slower than 2X of the fastest one gets 5% bonus score in the final grade.

Input Data

- First line contains 8 integers: N D x0 x1 A B C M
- For i >= 2
  - X[i] = (A * X[i - 1] + B * X[i - 2]+ C) % M
- For all i
  - X[i] /= M;

- N <= 10^5
- D <= 1600

Input Data

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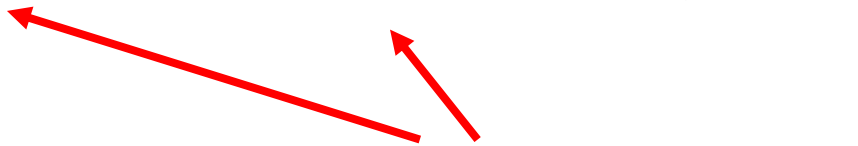

Caution the potential overflow here!

- N <= 10^5
- D <= 1600

Output Format

- D lines
- Each line contains a floating number
  - The logistic regression parameters

What Do We Need to Do?

- We are required to complete two scripts
- compiler.sh
  - it is executed once before the actual testing starts
- run.sh
  - it should takes two arguments, the first argument is the input file name, the second one is the file name that you should write your sorted results into.

Testing Environment

- ssh yourusername@granger.cs.rit.edu
- Intel(R) Xeon(R) CPU E5-2650 v4 @ 2.20GHz
- 48 threads in total (2 sockets, 12 cores per socket, 2 threads per core)
- 251 GB memory

- Testing limit:
  - 8 threads taskset -c

“Premature optimization is the root of all evil”

--- Sir Tony Hoare

GPU Computing

GPU (Graphics Processing Unit)

- Rendering
  - 3D surfaces
  - Textures
  - Lights
  - Views

https://en.wikipedia.org/wiki/File:Stanford_bunny_qem.png

https://en.wikipedia.org/wiki/Utah_teapot

https://www.quora.com/What-has-a-better-story-GTA-V-or-GTA-San-Andreas

GPU Rendering

- Direct3D
- OpenGL

- Use primitives to render a frame

GPU ~~Rendering~~ Computing (Before 2007)

- Direct3D
- OpenGL

- Use primitives to render a frame
- Make your 2D array as a frame and call render primitives

GPU Computing (After 2007)

- CUDA (~~Compute Unified Device Architecture~~)
- C/C++, Fortran
- GPGPU (General-Purpose computing on Graphics Processing Units)
- OpenCL

GPU Architecture

- 108 Streaming Multi-processor (SM)
- 40 GB High-Bandwidth Memory (HBM)
  - 1555 GB/sec
  - 6912 FP32 CUDA cores
- 432 Tensor Cores, TensorFloat-32(TF32) Dense Tensor (156 TFLOPs)
- 192KB * 108 L1 Cache
- 40960 KB L2 Cache

GPU Scheduling

- SIMT (Single Instruction Multiple Thread)
- Warp
- Dangerous to implement critical section (Pre Volta)

- Independent Thread Scheduling (After Volta)

CUDA Programming

- Kernel
- Grid
- Block
- Thread
- Warp

- Host Memory
- Device Memory
  - Global Memory
  - Shared Memory

CUDA Programming

```
__global__
void saxpy(int n, float a, float *x, float *y){
        int i = blockIdx.x * blockDim.x + threadIdx.x;
        if (i < n)
                y[i] = a * x[i] + y[i];
}
```

CUDA Programming

```
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        int i = blockIdx.x * blockDim.x + threadIdx.x;
        if (i < n)
                y[i] = a * x[i] + y[i];
}
saxpy<<<nB, nT>>>(n, a, x, y);
```

CUDA Programming


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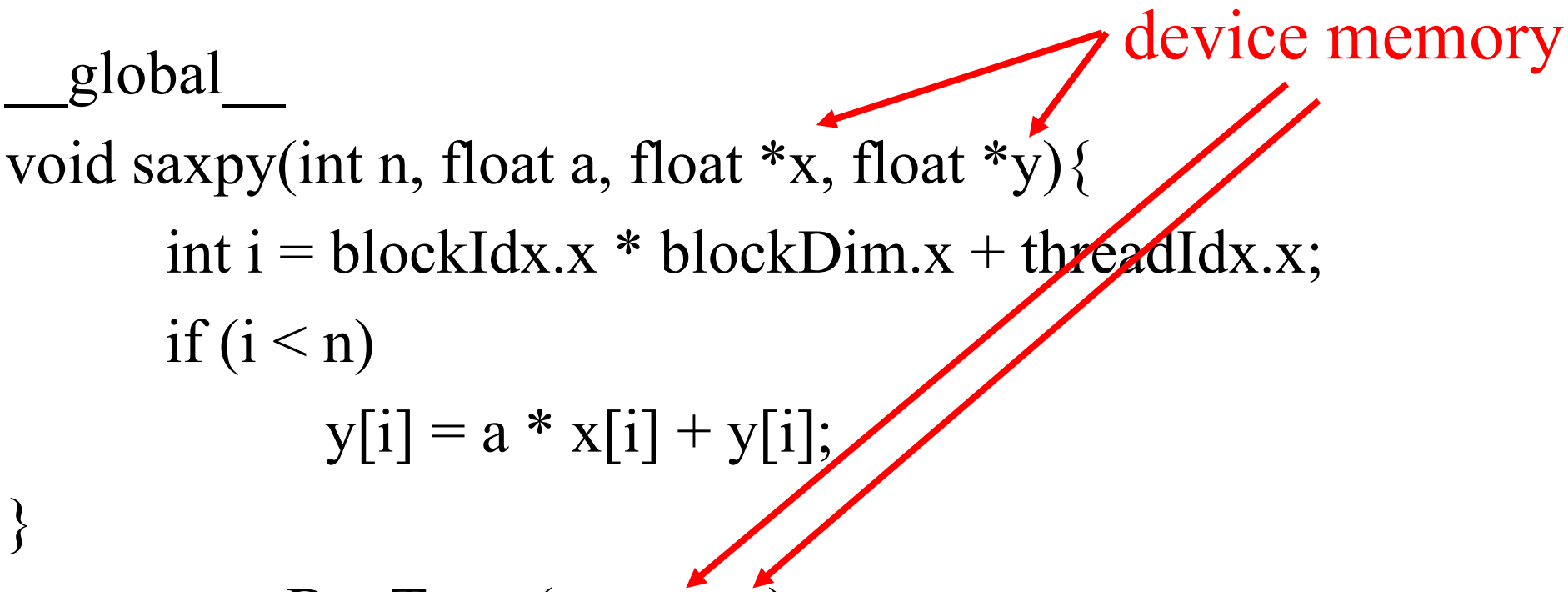
CUDA Programming



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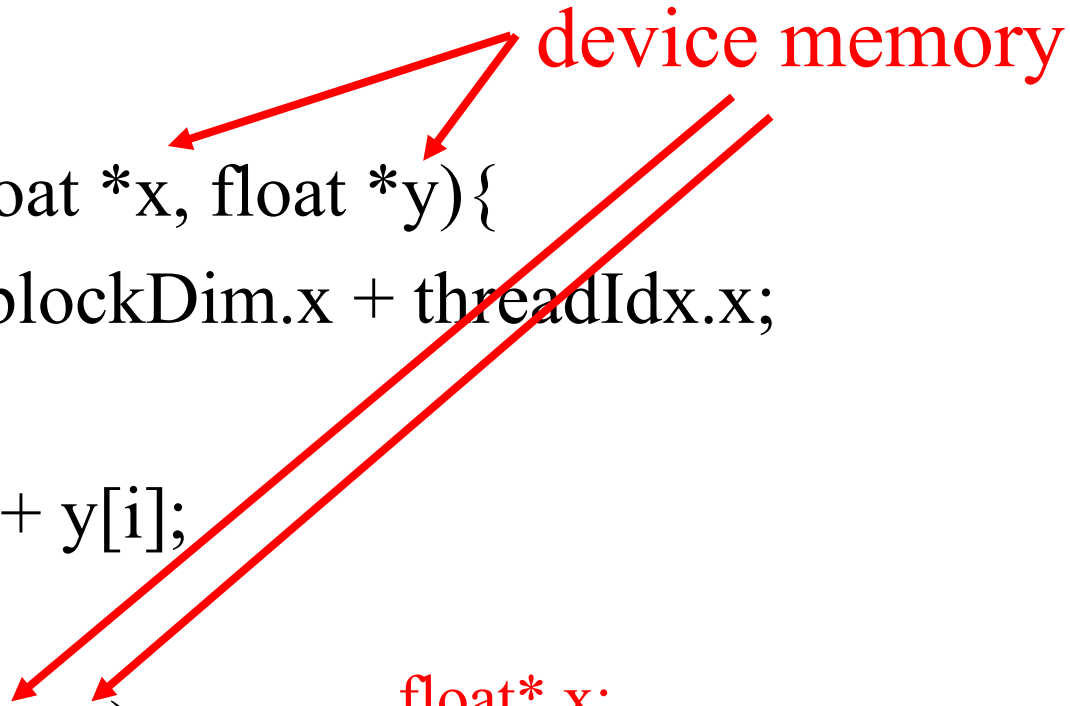


```
float* x;
cudaMalloc(&x, n * sizeof(float));
```

cudaError_t cudaMalloc (void** devPtr, size_t size)

Host Memory vs. Device Memory

- cudaMalloc, cudaFree
- cudaError_t cudaMemcpy (void* dst, const void* src, size_t count, cudaMemcpyKind kind)
  - cudaMemcpyHostToHost = 0
    - Host -> Host
  - cudaMemcpyHostToDevice = 1
    - Host -> Device
  - cudaMemcpyDeviceToHost = 2
    - Device -> Host
  - cudaMemcpyDeviceToDevice = 3
    - Device -> Device
  - cudaMemcpyDefault = 4
    - Direction of the transfer is inferred from the pointer values. Requires unified virtual addressing

CUDA Compilation

- nvcc a.cu -o a.out -O3 -Xptxas -O3
- cuda-gdb
  - -g -G (without optimizations)
  - info cuda threads
  - cuda thread 0
- cuda-memcheck
- nvprof
  - nvvp

Scan

- Inclusive scan
- Exclusive scan

- Naïve scan
- Work-efficient scan

```
__global__ void reduce(float *g_odata, float *g_idata, int n) {
  extern __shared__ float temp[];  // allocated on invocation
  int thid = threadIdx.x; int offset = 1;
  temp[2*thid] = g_idata[2*thid]; // load input into shared memory
  temp[2*thid+1] = g_idata[2*thid+1];
  for (int d = n>>1; d > 0; d >>= 1){  // build sum in place up the tree
    __syncthreads();
    if (thid < d)     {
      int ai = offset*(2*thid+1)-1;
      int bi = offset*(2*thid+2)-1;
      temp[bi] += temp[ai];
    }
    offset *= 2;
  }
  __syncthreads();
  if (thid == 0)
    *g_odata = temp[n-1];
}
```

```
__global__ void reduce(float *g_odata, float *g_idata, int n) {
  extern __shared__ float temp[]; // allocated on invocation
  int thid = threadIdx.x; int offset = 1;
  temp[2*thid] = g_idata[2*thid]; // load input into shared memory
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      temp[bi] += temp[ai];
    }
    offset *= 2;
  }
  __syncthreads();
  if (thid == 0)
    *g_odata = temp[n-1];
}
```

Dynamic shared memory allocation

```
reduce<<<1,nT,n>>>(d_out,d_in,n)
```

Shared memory size per block

Static:

```
__shared__ float temp[128];
```

```
__global__ void reduce(float *g_odata, float *g_idata, int n) {
  extern __shared__ float temp[];// allocated on invocation
  int thid = threadIdx.x; int offset = 1;
  temp[2*thid] = g_idata[2*thid]; // load input into shared memory
  temp[2*thid+1] = g_idata[2*thid+1];
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    __syncthreads();
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      temp[bi] += temp[ai];
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Dynamic shared memory allocation

reduce<<<1,nT,n>>>(d_out,d_in,n)

Shared memory size per block

Static:
__shared__ float temp[128];

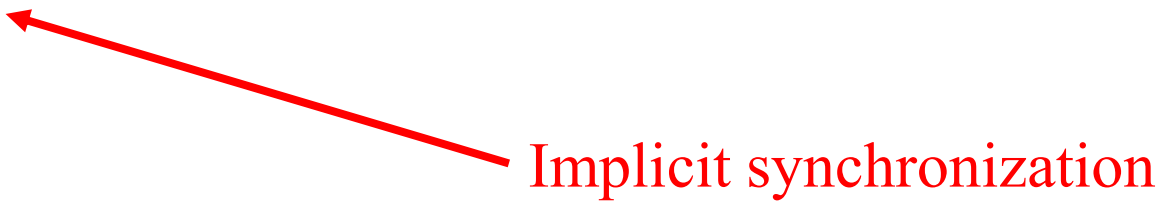
Device/Host Synchronization

```
reduce<<<1,nT,n>>>(d_sum,d_array,n);
for i = 0 to logn do
        sweep_down<<<1,nT,n>>>(d_array,n);

printf(“finished\n”);
cudaMemcpy(h_array,d_array,cudaMemcpyDeviceToHost);
printf(…);
```

Device/Host Synchronization

```
reduce<<<1,nT,n>>>(d_sum,d_array,n);
for i = 0 to logn do
        sweep_down<<<1,nT,n>>>(d_array,n);
cudaDeviceSynchronize();
printf("finished\n");
cudaMemcpy(h_array,d_array,cudaMemcpyDeviceToHost);
printf(…);
```



CUDA Kernel Launch

- kernel_name<<<nB,nT,shared_memory_size,stream>>>(…)

- cudaStream_t stream
- cudaStreamCreate(&stream)
- cudaMemcpyAsync(dst,src,size,stream)
- cudaStreamSynchronize(stream)

- Default stream: 0

Multiple GPU Support

- CUDA_VISIBLE_DEVICES
- cudaError_t cudaSetDevice (int device)
- __host__ _device__ cudaError_t cudaMalloc (void** devPtr, size_t size)
- __host__ cudaError_t cudaMemcpyPeer (void* dst, int dstDevice, const void* src, int srcDevice, size_t count)
- __host__ cudaError_t cudaMemcpyPeerAsync (void* dst, int dstDevice, const void* src, int srcDevice, size_t count, cudaStream_t stream = 0)