## Introduction to Computer Science Theory (4003-380-01) Prof. Richard Zanibbi (20103, Spring 2011) Homework 7, Due 4pm, Tuesday May 3, 2011

All questions are written for this assignment; submit them through myCourses or on paper before the start of class. If you work in a group of two, submit your answers only once, and make sure to include both your names on your submitted work.

## Questions (40 points in total)

- 1. Consider the Turing machine  $M_1$ , defined and illustrated in Example 3.9 in the course textbook. Provide the sequence of configurations that  $M_1$  enters when started on the input strings below. Please write the configurations as a list, with one configuration per line.
  - (a) 1##1
  - (b) 10#10
- 2. Show that decidable languages are closed under the operations of:
  - (a) Complement
  - (b) Intersection
- 3. Give a formal definition of an enumerator. Use a two-tape Turing machine, which uses its second tape as a printer. Provide a definition of the enumerated language.
- 4. Express the problem of determining whether a DFA and a regular expression are equivalent, using a language of strings accepted by a Turing machine. Demonstrate that this problem is decidable.
- 5. Let  $INFINITE_{PDA} = \{\langle M \rangle \mid M \text{ is a PDA and } L(M) \text{ is infinite}\}$ . Show that  $INFINITE_{PDA}$  is decidable. (see related Question 4.9 in the textbook)