



# CSCI 742 - Compiler Construction

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Lecture 38

Register Allocation

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# Register Machines

- Debate topic: stack or register architecture?

see e.g. Yunhe Shi et al. “Virtual Machine Showdown: Stack Versus Registers”  
ACM Transactions on Architecture and Code Optimization, Vol. 4, No. 4, 2008

Register Machines Benefit:

- Closer to modern CPUs (RISC architecture) and control-flow graphs

Examples:

- RISC: ARM architecture, RISC-V
- CISC: x86 architecture

Directly Addressable RAM

Large - GB, slow even with cache

Few fast  
Registers

R<sub>0</sub>

R<sub>1</sub>

R<sub>2</sub>

...

R<sub>31</sub>

# Basic Instructions of Register Machines

- $R_i \leftarrow \text{Mem}[R_j]$       load
- $\text{Mem}[R_j] \leftarrow R_i$       store
- $R_i \leftarrow R_j \oplus R_k$       compute: for an operation  $\oplus$

Efficient register machine code uses as few loads and stores as possible

# State Mapped to Register Machine

Both dynamically allocated heap and stack expand

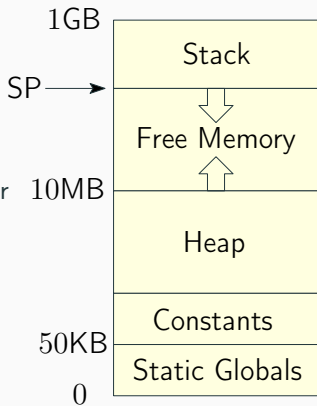
- Heap need not be contiguous; can request more memory from the OS if needed
- Stack grows downwards

Heap is more general:

- Can allocate, read/write, and deallocate, in any order
- Garbage Collector does deallocation automatically
  - Must be able to find free space among used one, group free blocks into larger ones (compaction),...

Stack is more efficient:

- Allocation is simple: increment, decrement
- Top of stack pointer (SP) is often a register
- If stack grows towards smaller addresses:
  - to allocate  $N$  bytes on stack (push):  $SP := SP - N$
  - to deallocate  $N$  bytes on stack (pop):  $SP := SP + N$



( Exact picture may depend on hardware and operating system )

# JVM vs. General Register Machine Code

- Naïve Correct Translation

JVM:

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`imul`

Register Machine:

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$R_1 \leftarrow \text{Mem}[\text{SP}]$

$\text{SP} = \text{SP} + 4$

$R_2 \leftarrow \text{Mem}[\text{SP}]$

$R_2 \leftarrow R_1 * R_2$

$\text{Mem}[\text{SP}] \leftarrow R_2$

# Using Registers

- Variables usually refer to memory
  - `&x` yields a memory location
  - Need to load variables into registers to perform operations on them
1. Load from memory into registers
  2. Perform operation on registers
  3. Store results from registers back to memory

## Example: How many variables?

- Do we need 7 distinct registers if we wish to avoid load and stores?
- Variables:  $x$  ,  $y$  ,  $z$  ,  $xy$  ,  $yz$  ,  $xz$  ,  $r$

```
x = m[0];
```

```
y = m[1];
```

```
xy = x * y;
```

```
z = m[2];
```

```
yz = y*z;
```

```
xz = x*z;
```

```
r = xy + yz;
```

```
m[3] = r + xz;
```

## Example: How many variables?

- Do we need 7 distinct registers if we wish to avoid load and stores?
- Variables:  $x$ ,  $y$ ,  $z$ ,  $xy$ ,  $yz$ ,  $xz$ ,  $r$

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xy = x * y;
z = m[2];
yz = y*z;
xz = x*z;
r = xy + yz;
m[3] = r + xz;
```

```
x = m[0];
y = m[1];
xy = x * y;
z = m[2];
yz = y*z;
y = x*z; // reuse y
x = xy + yz; // reuse x
m[3] = x + y;
```

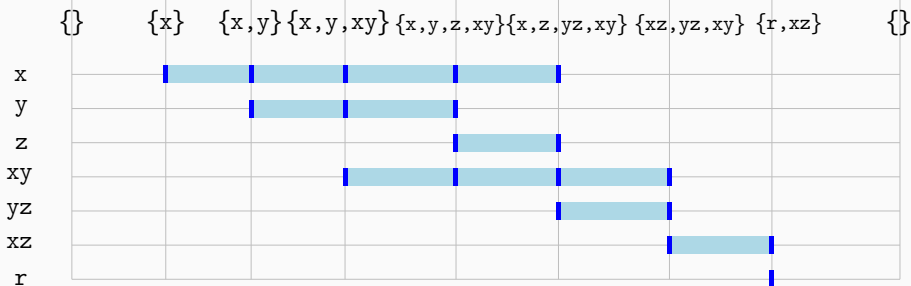
- Can do it with 5 only!



# Idea of Register Allocation

program: `x=m[0];y=m[1]; xy=x*y; z=m[2] ; yz=y*z ; xz=x*z ; r=xy+yz;m[3]=r+xz`

live variable analysis result:

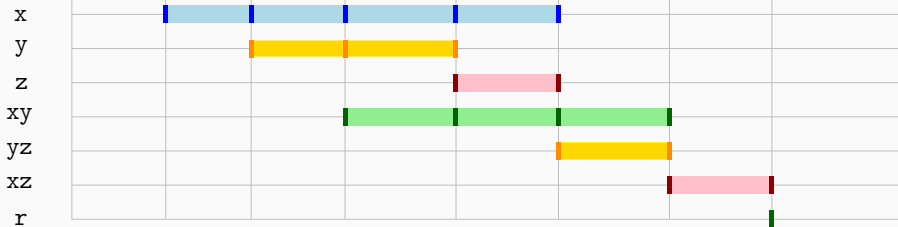


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live variable analysis result:

{ }      {x}      {x,y} {x,y,xy} {x,y,z,xy} {x,z,yz,xy} {xz,yz,xy} {r,xz}      { }



R<sub>1</sub>

R<sub>2</sub>

R<sub>3</sub>

R<sub>4</sub>

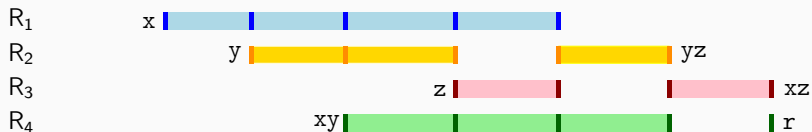
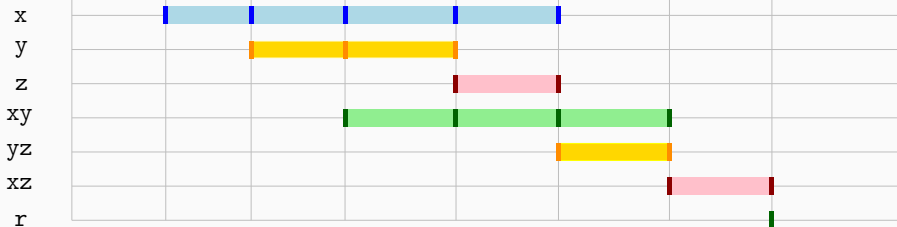
- Each color denotes a register
- Avoid overlap of same colors
- 4 registers are enough for this 7-variable program

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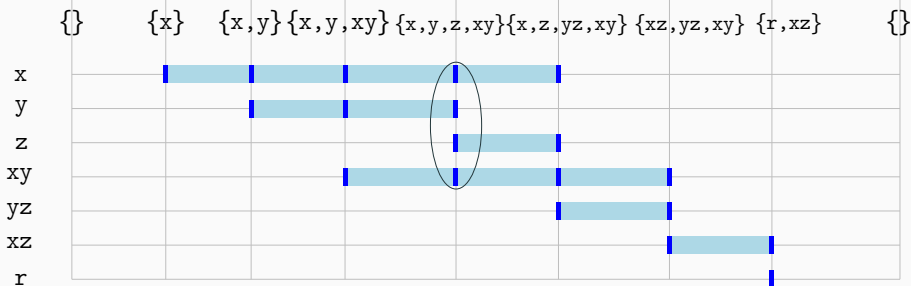


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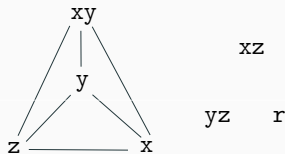
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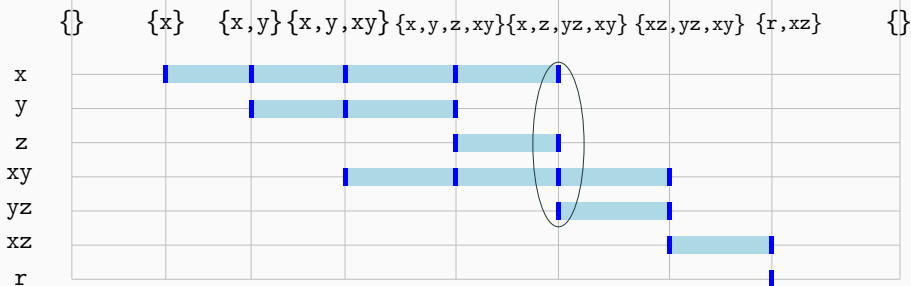
- For each pair of variables determine if there is a point at which they are both alive
- Construct interference graph



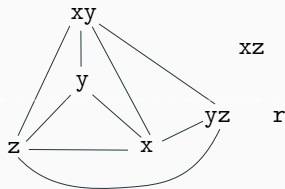
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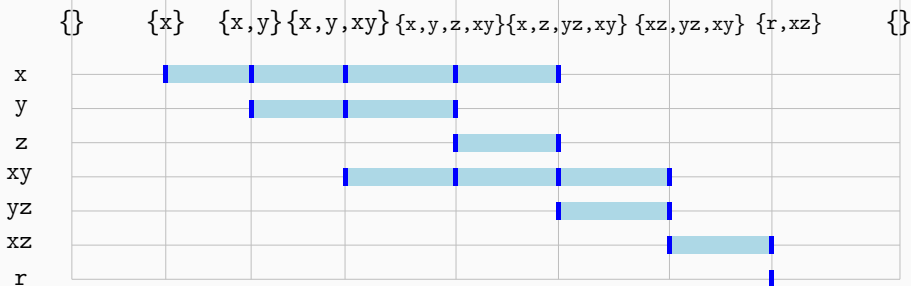
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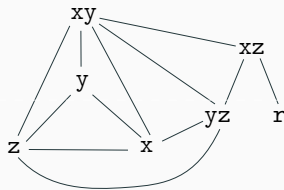
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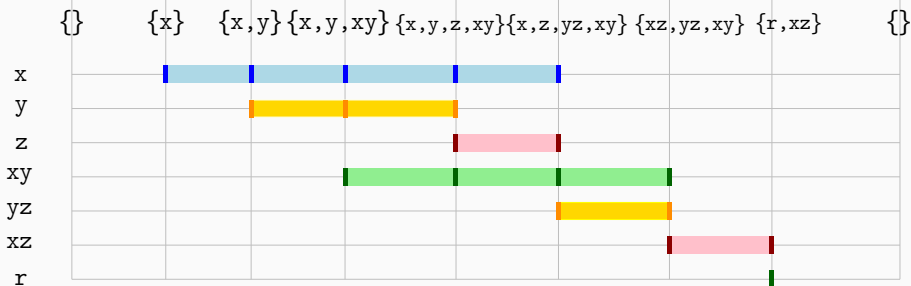
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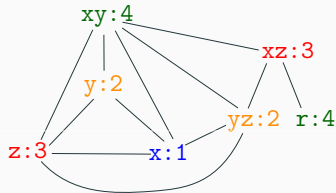
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live variable analysis result:



- Need to assign colors (register numbers) to nodes such that:
- If there is an edge between nodes, then those nodes have different colors
- Standard graph vertex coloring problem

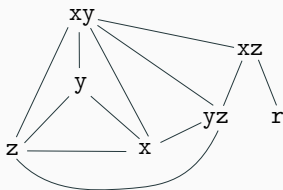


# Register Interference Graph (RIG)

- Indicate whether there exists a point of time where both variables are alive
- Look at the sets of live variables at all program points after running live-variable analysis
- If two variables occur together, draw an edge
- We aim to assign different registers to such these variables
- Finding assignment of variables to  $K$  registers:  
corresponds to coloring graph using  $K$  colors



# Graph Coloring Problem



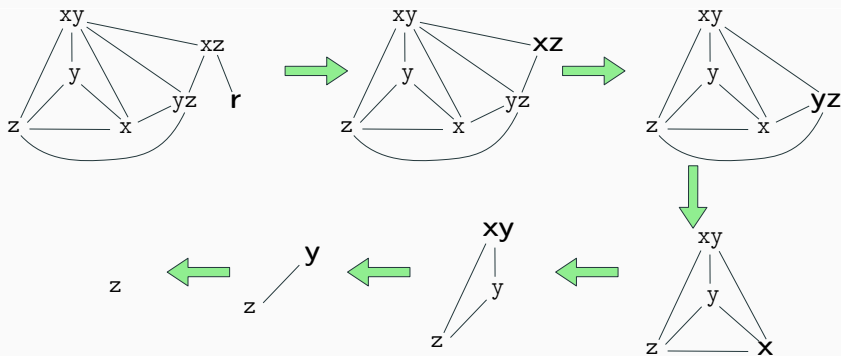
- NP hard
- In practice, there are heuristics that work for typical graphs
- If we cannot fit it all variables into registers, perform a **spill**:  
Store variable into memory and load later when needed

# Heuristic for Coloring with $K$ Colors

## Simplify:

- If there is a node with less than  $K$  neighbors, we will always be able to color it!
- So we can remove such node from the graph
  - (if it exists, otherwise remove other node)
- This reduces graph size. It is useful, even though incomplete

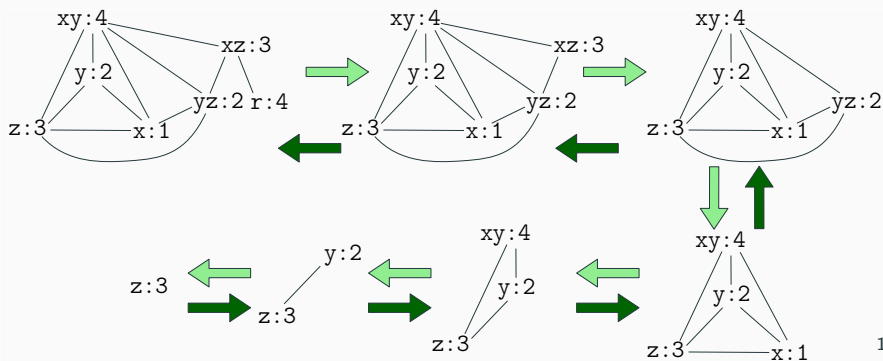
(e.g. can color planar by at most 4 colors, yet can have nodes with many neighbors)



# Heuristic for Coloring with $K$ Colors

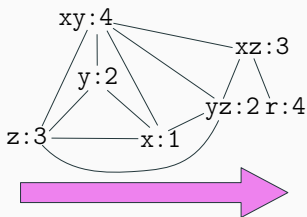
## Select:

- Assign colors backwards, adding nodes that were removed
- If the node was removed because it had  $< K$  neighbors, we will always find a color
- If there are multiple possibilities, we can choose any color



## Use Computed Registers

```
x = m[0];  
y = m[1];  
xy = x * y;  
z = m[2];  
yz = y*z;  
xz = x*z;  
r = xy + yz;  
m[3] = res1 + xz;
```



```
R1 = m[0]  
R2 = m[1]  
R4 = R1 * R2  
R3 = m[2]  
R2 = R2 * R3  
R3 = R1 * R3  
R4 = R4 + R2  
m[3] = R4 + R3
```

# Summary of Heuristic for Coloring

## **Simplify (forward, safe):**

If there is a node with less than  $K$  neighbors, we will always be able to color it, so we can remove it from the graph

## **Potential Spill (forward, speculative):**

If every node has  $K$  or more neighbors, we still remove one of them we mark it as node for potential spilling. Then remove it and continue

## **Select (backward):**

Assign colors backwards, adding nodes that were removed

- If we find a node that was spilled, we check if we are lucky, that we can color it. If yes, continue
- If not, insert instructions to save and load values from memory

## **(actual spill)**

Restart with new graph

(graph is now easier to color as we killed a variable)